
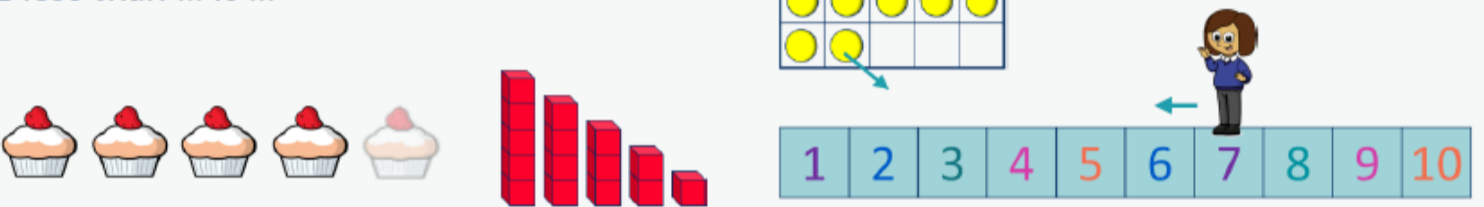

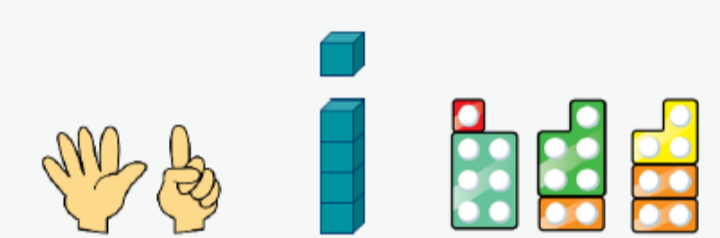

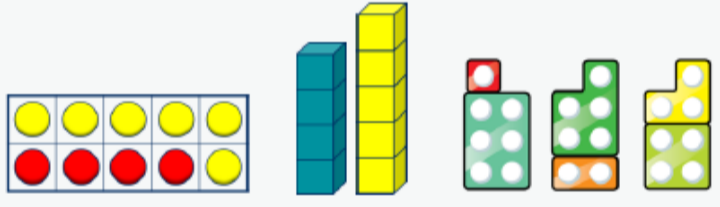

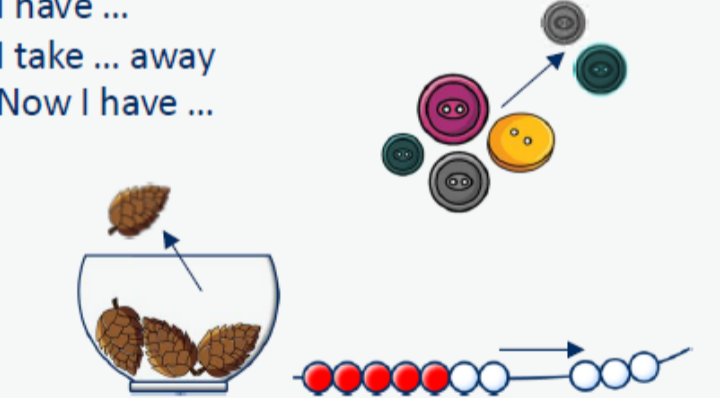
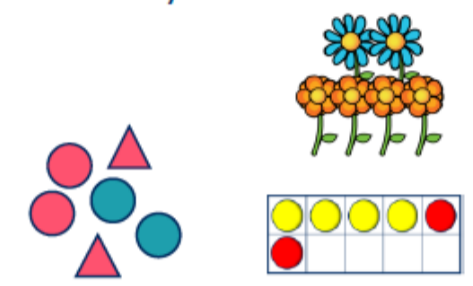
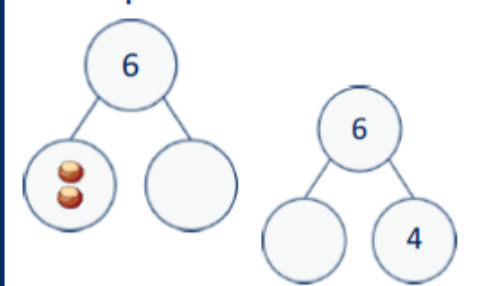
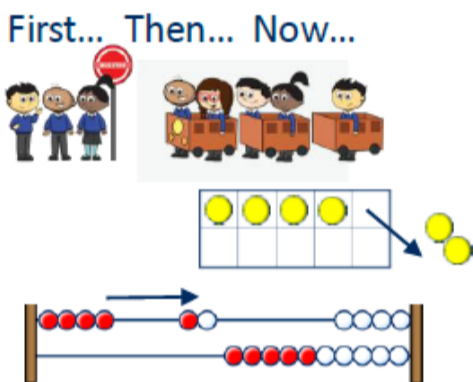
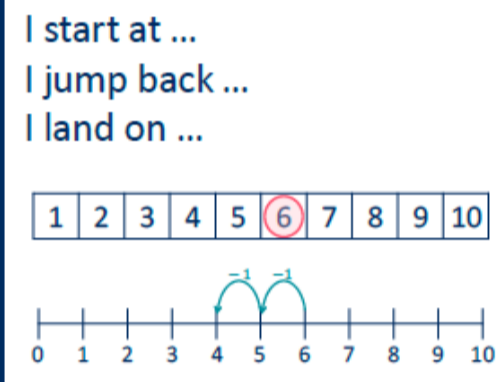
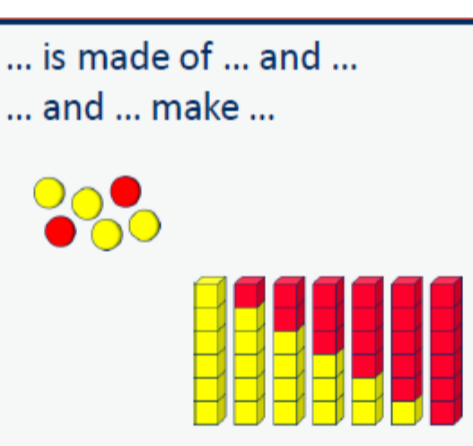
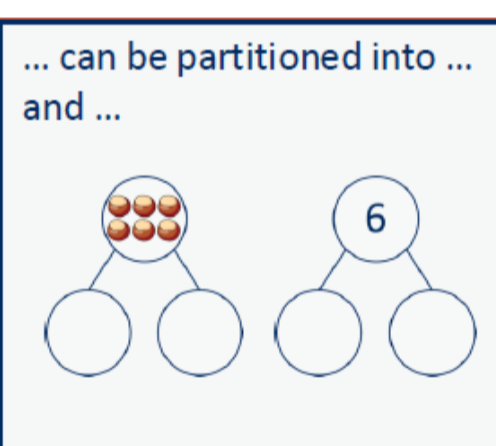
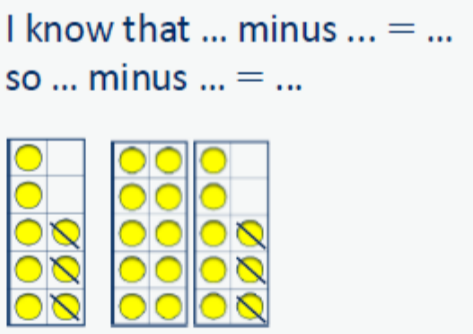
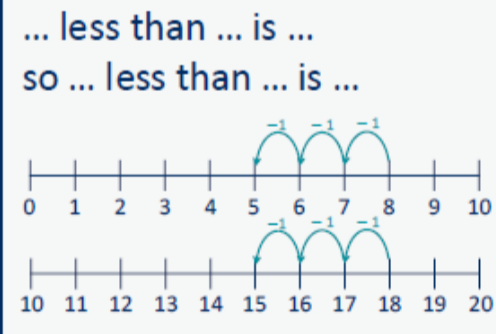

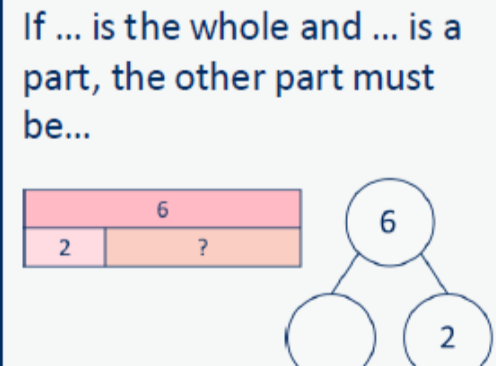



Subtraction

<p>Reception</p>	<ul style="list-style-type: none"> Have a deep understanding of number to 10, including the composition of each number. Subitise (recognise quantities without counting) up to 5 Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (and some subtraction facts) and some number bonds to 10, including double facts. 	
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Conceptually subitise to 5</p> <p>Notice the parts that make up the whole.</p>	<p>What do you see? How do you see it?</p> 	
<p>1 less</p> <p>Continue to link to stories, songs and rhymes.</p>	<p>1 less than ... is ...</p> 	
<p>Notice the composition of numbers within 10</p> <p>Link to stories, songs and rhymes.</p>	<p>How many...? How many...? How many altogether?</p> 	<p>How many ways can you make...?</p> 
<p>Partition</p> <p>Using objects, explore different ways to partition a number into 2 or more parts.</p>	<p>There are ... altogether. I can see ... here and ... there.</p> 	<p>... and ... make ...</p> 
<p>Take away</p> <p>A quantity is reduced.</p>	<p>First... Then... Now...</p> 	<p>I have ... I take ... away Now I have ...</p> 

Subtraction

<p>Year 1</p>	<ul style="list-style-type: none"> Read, write and interpret mathematical statements involving subtraction (−) and equals (=) signs. Represent and use number bonds and related subtraction facts within 20 Subtract one-digit and two-digit numbers to 20, including zero. Solve one-step problems that involve subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \square - 9$ 		
<p>Progression of skills</p>	<p>Key representations</p>		
<p>Find a part</p> <p>Link to number bonds and known facts. E.g. $2 + 4 = 6$ so if 6 is the whole and 4 is a part, the other part must be 2</p>	<p>There are ... in total. ... are ... How many are not ...?</p> 	<p>... is the whole. ... is a part. ... is a part.</p> 	<p>... subtract ... is equal to is equal to ... − ...</p> $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$
<p>Take away</p> <p>A quantity is decreased.</p>	<p>First... Then... Now...</p> 	<p>I start at ... I jump back ... I land on ...</p> 	<p>... minus ... is equal to is equal to ... − ...</p> $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$
<p>Bonds within 10</p> <p>Focus on subtraction facts.</p> <p>Encourage children to notice patterns.</p>	<p>... is made of ... and and ... make ...</p> 	<p>... can be partitioned into ... and ...</p> 	<p>... minus ... is equal to ...</p> $6 - 0 = 6$ $6 - 1 = 5$ $6 - 2 = 4$ $6 - 3 = 3$ $6 - 4 = 2$ $6 - 5 = 1$ $6 - 6 = 0$
<p>Related facts within 20</p> <p>Make links to known facts.</p>	<p>I know that ... minus ... = ... so ... minus ... = ...</p> 	<p>... less than ... is ... so ... less than ... is ...</p> 	<p>What patterns do you notice?</p> $8 - 3 = 5$ $18 - 3 = 15$ $5 = 8 - 3$ $15 = 18 - 3$
<p>Missing numbers</p> <p>Make links to known facts.</p>	<p>How many do you need to subtract to make ...?</p> 	<p>If ... is the whole and ... is a part, the other part must be...</p> 	<p>... minus ... is equal to ...</p> $6 - \square = 2$ $2 = 6 - \square$ 

Subtraction

- Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100
- Subtract numbers using concrete objects, pictorial representations, and mentally, including:
 - a two-digit number and 1s
 - a two-digit number and 10s
 - 2 two-digit numbers
- Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.

Progression of skills | **Key representations**

Subtract ones from any number (related facts)
Make links to known facts.

I know that ... minus ... = ...
so ... minus ... = ...

... less than ... is ...
so ... less than ... is ...

What do you notice?
Can you continue the pattern?

$8 - 3 = 5$
 $18 - 3 = 15$
 $28 - 3 = 25...$

Subtract across a 10
Partition the number being subtracted to bridge through a ten.

... can be partitioned into ... and ...

Make links with related facts.

$13 - 5$

$33 - 5$

Subtract multiples of 10
Make links to known facts within ten.

... ones - ... ones = ... ones
so ... tens - ... tens = ... tens

What is the same?
What is different?

$5 - 2 = 3$
 $50 - 20 = 30$

Subtract 10s from any number
Make links to known facts.

... tens - ... tens = ... tens
... tens and ... ones = ...

To subtract ... I need to subtract 10 ... times.

I know that ... minus ... = ...
so ... minus ... = ...

$50 - 20 = 30$
 $54 - 20 = 34$

Subtract two 2-digit numbers (not across a ten)

... ones - ... ones = ... ones
... tens - ... tens = ... tens

$43 - 21$

$3 \text{ ones} - 1 \text{ one} = 2 \text{ ones}$
 $4 \text{ tens} - 2 \text{ tens} = 2 \text{ tens}$
 $2 \text{ tens and } 2 \text{ ones} = 22$

Subtract two 2-digit numbers (across a ten)
Begin to exchange 1 ten for 10 ones.

I need to make an exchange because I do not have enough ones to subtract ... ones.

$43 - 25$

$3 \text{ ones} - 5 \text{ ones}$
(I need to exchange 1 ten for 10 ones)

$13 \text{ ones} - 5 \text{ ones} = 8 \text{ ones}$
 $3 \text{ tens} - 2 \text{ tens} = 1 \text{ ten}$
 $1 \text{ ten and } 8 \text{ ones} = 18$

Missing numbers
Solve missing number problems and use the inverse to check.

How many do you need to subtract to make ...?

If ... is a whole and ... is a part, then ... is the other part.

... can be partitioned into ... and ...

$10 - \square = 6$
 $6 + \square = 10$

$7 - 3 = \square$
 $\square + 3 = 7$

$18 - \square = 12 + 2$

Subtraction

Year 3	<ul style="list-style-type: none"> Subtract numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds. Subtract numbers with up to three digits, using formal written methods. Subtract fractions with the same denominator within 1 whole.
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Progression of skills	Key representations
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Subtract 1s, 10s and 100s from a 3-digit number	<p>The ones/tens/hundreds column will decrease by ...</p> <table border="1"> <tr> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> <tr> <td></td> <td></td> <td></td> </tr> </table> <p>444 - 2 = 777 - 4 =</p> <p>444 - 20 = 777 - 40 =</p> <p>444 - 200 = 777 - 400 =</p>	Hundreds	Tens	Ones				<p>What patterns do you notice?</p> <p>235 - 3 =</p> <p>235 - 30 =</p> <p>235 - 300 =</p> <p>118 - <input type="text"/> = 111</p> <p>624 - 20 = 181 - <input type="text"/> = 111</p> <p>654 - 50 = 811 - <input type="text"/> = 111</p> <p>694 - 90 =</p>
Hundreds	Tens	Ones						

Subtract two numbers (no exchange)	<p>... ones - ... ones = ... ones</p> <p>... tens - ... tens = ... tens</p> <p>... hundreds - ... hundreds = ... hundreds</p> <p>Mental strategies and introduction of formal written method.</p>
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Subtract two numbers across a 10 or 100	<p>I need to subtract ... ones. I do/do not need to make an exchange.</p> <p>I need to subtract ... tens. I do/do not need to make an exchange.</p> <p>I can exchange 1 ... for 10 ...</p> <p>Formal written method involving up to 2 exchanges including 3-digit subtract 2-digit numbers.</p>
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Complements to 100	<p>100 minus ... is equal to ...</p> <p>Focus on subtraction facts.</p> <p>Encourage children to notice patterns.</p>	<p>I subtract ... tens, then I subtract ... ones.</p> <p>100 - 38 = 62</p> <p>100 - 62 = 38</p> <p>62 = 100 - 38</p> <p>38 = 100 - 62</p>
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Subtract fractions with the same denominator within 1 whole	<p>When subtracting fractions with the same denominator, I only subtract the numerator.</p> <p>... fifths - ... fifths = ... fifths</p> <p>5/5 - 1/5</p> <p>4/5 - 1/5</p> <p>3/5 - 1/5</p> <p>Make links with known facts.</p>
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Subtraction

Year 5	<ul style="list-style-type: none"> Subtract whole numbers with more than 4 digits. Subtract numbers mentally with increasingly large numbers. Subtract decimals, including a mix of whole numbers and decimals, decimals with different numbers of decimal places, and complements of 1 Subtract fractions with the same denominator, and denominators that are multiples of the same number.
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Progression of skills	Key representations
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Subtract whole numbers with more than 4 digits	I can exchange 1 ... for 10 ...
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Encourage children to estimate and use inverse operations to check answers to calculations.

Subtract using mental strategies	To subtract ..., I can subtract ... then add ...
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Subtract 1s, 10s, 100s etc from any number. Use number bonds and related facts.

Subtract decimals with up to 2 decimal places	
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Progress from the same number of decimal places to a different number of decimal places and from no exchange to exchange.

Complements to 1	
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Encourage children to make links with bonds to 10 and complements to 100 and 1,000 when finding a missing part or subtracting from 1

10	100
3 ?	35 ?
1	1
0.3 ?	0.35 ?

Subtract fractions with denominators that are a multiple of one another	The denominator has been multiplied by ..., so the numerator needs to be multiplied by... for the fractions to be equivalent.
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Convert fractions to the same denominator before subtracting. Progress from subtracting fractions within 1 whole to subtracting from a mixed number.

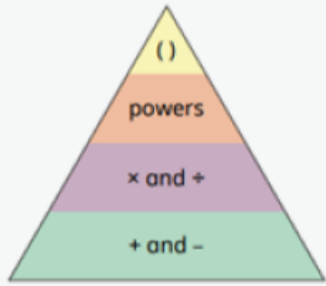
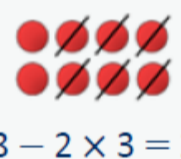

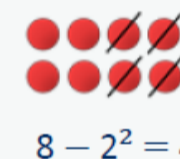
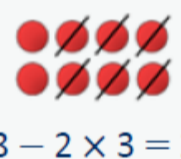

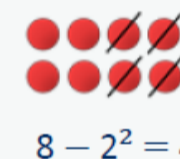
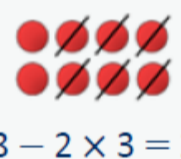

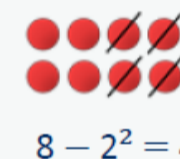
Subtraction



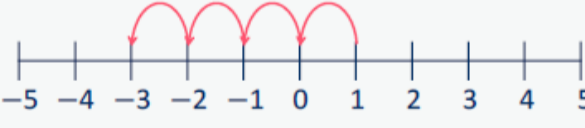
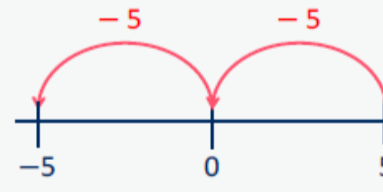
Year 6	<ul style="list-style-type: none"> Subtract larger numbers, using the formal written methods of columnar subtraction. Use their knowledge of the order of operations to carry out calculations involving the 4 operations. Calculate intervals across zero. Subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions.
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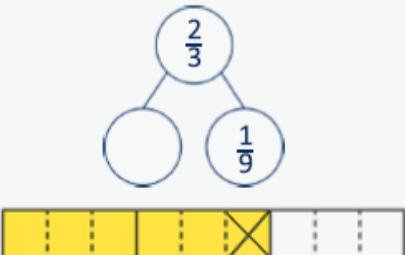
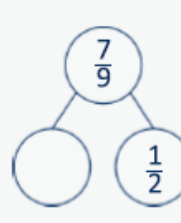
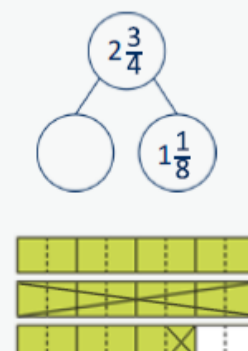
Progression of skills	Key representations
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Subtract integers up to 10 million	<table border="1" style="display: inline-table; margin-right: 20px;"> <tr><td>2</td><td>3</td><td>1</td><td>4</td><td>5</td><td>1</td><td>2</td><td>1</td></tr> <tr><td>-</td><td>1</td><td>8</td><td>4</td><td>3</td><td>2</td><td>1</td><td></td></tr> <tr><td></td><td>1</td><td>6</td><td>1</td><td>9</td><td>0</td><td>0</td><td></td></tr> </table> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><td colspan="3">4,604</td></tr> <tr><td>2,354</td><td>750</td><td>?</td></tr> </table> <table border="1" style="display: inline-table;"> <tr><td>8</td><td></td><td>4</td><td>8</td><td>5</td><td></td></tr> <tr><td>-</td><td>3</td><td>6</td><td></td><td></td><td>4</td></tr> <tr><td></td><td>5</td><td>5</td><td>5</td><td>5</td><td>5</td></tr> </table>	2	3	1	4	5	1	2	1	-	1	8	4	3	2	1			1	6	1	9	0	0		4,604			2,354	750	?	8		4	8	5		-	3	6			4		5	5	5	5	5
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Subtract decimals with up to 3 decimal places	<p>I do/do not need to make an exchange because ...</p> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><td>6</td><td>7</td><td>1</td><td>3</td></tr> <tr><td>-</td><td>1</td><td>3</td><td>4</td></tr> <tr><td></td><td>5</td><td>3</td><td>9</td></tr> </table> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><td>0</td><td>Tth</td><td>Hth</td><td>Thth</td></tr> <tr><td>0</td><td>9</td><td>7</td><td>5</td></tr> </table> <table border="1" style="display: inline-table;"> <tr><td>0</td><td>1</td><td>5</td><td>1</td><td>5</td></tr> <tr><td>-</td><td>0</td><td>6</td><td>4</td><td></td></tr> <tr><td></td><td>0</td><td>9</td><td>7</td><td>5</td></tr> </table>	6	7	1	3	-	1	3	4		5	3	9	0	Tth	Hth	Thth	0	9	7	5	0	1	5	1	5	-	0	6	4			0	9	7	5
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Order of operations	<p>... has greater priority than ... , so the first part of the calculation I need to do is ...</p> <div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> <table border="0"> <tr> <td style="text-align: center;">  $8 - 2 \times 3 = 2$ </td> <td style="text-align: center;">  $(8 - 2) \times 3 = 18$ </td> <td style="text-align: center;">  $8 - 2^2 = 4$ </td> </tr> </table> </div> </div>	 $8 - 2 \times 3 = 2$	 $(8 - 2) \times 3 = 18$	 $8 - 2^2 = 4$
 $8 - 2 \times 3 = 2$	 $(8 - 2) \times 3 = 18$	 $8 - 2^2 = 4$		

Negative numbers	<p>... minus ... is equal to ...</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;">  $-1 - 4 = -5$ </div> <div style="text-align: center;">  The difference between -5 and -1 is 4 </div> </div> <div style="display: flex; justify-content: space-around; margin-top: 20px;"> <div style="text-align: center;">  $1 - 4 = -3$ </div> <div style="text-align: center;">  The difference between 5 and -5 is 10 </div> </div>
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Subtract fractions	<p>The denominator has been multiplied by ... , so the numerator needs to be multiplied by...</p> <div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> $\frac{2}{3} - \frac{1}{9} = \frac{6}{9} - \frac{1}{9} = \frac{5}{9}$ </div> </div>	<p>The lowest common multiple of ... and ... is ...</p> <div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> $\frac{7}{9} - \frac{1}{2} = \frac{14}{18} - \frac{9}{18} = \frac{5}{18}$ </div> </div>	<p>... is made up of ... wholes and ...</p> <div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> $2\frac{3}{4} - \frac{1}{8} = 1\frac{5}{8}$ </div> </div>
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